

Lecture #10 Modeling of General Electrochemical Processes and Electrochemical Methods of Research

Goal

This lecture introduces students to the modeling of general electrochemical processes, including charge transfer, mass transport, and equilibrium thermodynamics. In addition, it provides an overview of two essential electrochemical research methods - cyclic voltammetry (CV) and electrochemical impedance spectroscopy (EIS) highlighting how they are modeled and interpreted to extract meaningful kinetic and transport parameters.

Introduction

Electrochemical processes are central to a wide range of scientific and industrial applications, including energy storage, catalysis, and sensor development. These processes involve electron transfer at interfaces, coupled with mass transport, and sometimes chemical reactions.

This lecture focuses on modeling general electrochemical processes and discusses two key experimental methods: cyclic voltammetry (CV) and electrochemical impedance spectroscopy (EIS). These methods provide insights into reaction mechanisms, kinetic parameters, and system properties.

General Electrochemical Processes

Electrochemical processes involve the interaction of species in solution with an electrode surface. Key phenomena include charge transfer, mass transport, and coupled chemical reactions.

The modeling of these processes often uses the following fundamental equations:

- Nernst Equation: Relates the equilibrium potential to the concentrations of reactants and products.

- Butler-Volmer Equation: Describes the current density (j) as a function of overpotential (η):

$$j = j_0 [\exp(\alpha F \eta / RT) - \exp(-\beta F \eta / RT)]$$

j_0 : Exchange current density, α , β : Transfer coefficients, F : Faraday's constant, R : Gas constant, T : Temperature.

- Mass Transport Equations: Combine diffusion, convection, and migration contributions using the Nernst-Planck equation.

Cyclic Voltammetry (CV)

Cyclic voltammetry is a dynamic electrochemical technique where the electrode potential is swept linearly with time, and the resulting current is measured. It provides information on redox processes, reaction kinetics, and diffusion coefficients.

Key aspects of CV modeling include:

- Randles-Sevcik Equation: Predicts peak current (i_p) for reversible reactions:

$$i_p = (2.69 \times 10^5) n^{3/2} A D^{1/2} C v^{1/2}$$

n : Number of electrons, A : Electrode area, D : Diffusion coefficient, C : Concentration, v : Scan rate.

- Peak Shape and Separation: Help determine reversibility. A reversible reaction shows symmetric peaks with a 60 mV separation per electron at room temperature.

Applications: CV is used to study reaction mechanisms, characterize catalysts, and investigate redox-active materials.

Electrochemical Impedance Spectroscopy (EIS)

EIS measures the response of an electrochemical system to a small amplitude AC signal over a range of frequencies. It provides insights into resistance, capacitance, and diffusion processes.

Key modeling aspects include:

- **Equivalent Circuits:** Represent the system with resistors, capacitors, and constant phase elements (CPEs). For example, the Randles circuit models charge transfer and diffusion.
- **Nyquist and Bode Plots:** Visualize impedance data. Nyquist plots show imaginary versus real impedance, while Bode plots display magnitude and phase versus frequency.
- **Warburg Impedance:** Accounts for diffusion-controlled processes, with impedance scaling as $Z \propto \omega^{-1/2}$ at low frequencies.

Applications: EIS is widely used in battery characterization, corrosion studies, and electrode surface analysis.

Example Problem

A CV experiment for a reversible redox reaction produces a peak current of 150 μA at a scan rate of 50 mV/s. Given that $n = 1$, $A = 0.1 \text{ cm}^2$, and $C = 1 \text{ mM}$, estimate the diffusion coefficient (D).

Solution:

Using the Randles-Sevcik equation:

$$i_p = (2.69 \times 10^5) n^{3/2} A D^{1/2} C v^{1/2}$$

Rearrange to find D , and substitute the given values to calculate.

Summary

Modeling electrochemical processes involves understanding charge transfer, mass transport, and coupled reactions. Cyclic voltammetry and electrochemical impedance spectroscopy are powerful methods for probing system behavior, providing valuable insights for both fundamental and applied research.

Students are encouraged to practice interpreting CV and EIS data for real-world systems.

Learning Outcomes

By the end of this lecture, students will be able to:

- 1. Explain the fundamental equations used to model electrochemical processes (Nernst, Butler–Volmer, Nernst–Planck) (related to LO 4, ID 4.3–4.4).*
- 2. Model redox reactions by integrating thermodynamics, kinetics, and mass-transport principles (related to LO 4, ID 4.4–4.5).*
- 3. Interpret cyclic voltammograms and relate peak currents, peak separations, and shapes to reaction reversibility and diffusion control (related to LO 4, ID 4.4).*
- 4. Analyze EIS spectra (Nyquist and Bode plots), identifying charge-transfer resistance, double-layer capacitance, and diffusion behavior (related to LO 4, ID 4.4–4.5).*
- 5. Apply equivalent circuit models (e.g., Randles circuit) to extract kinetic parameters from impedance data (related to LO 4, ID 4.4–4.5).*
- 6. Evaluate the use of CV and EIS in studying catalysts, battery electrodes, corrosion, and other electrochemical systems (related to LO 4, ID 4.6–4.7).*

Questions and Self-Study Assignments

- 1. Write the Nernst equation and explain how concentration affects equilibrium potential.*
- 2. Derive the Butler–Volmer equation expression for small overpotentials (hint: linearization).*
- 3. Explain how the shape of a cyclic voltammogram indicates reaction reversibility.*
- 4. What information can be extracted from the semicircle of a Nyquist plot?*
- 5. Describe the physical meaning of Warburg impedance.*
- 6. Using the Randles–Ševčík equation, calculate the diffusion coefficient from the example problem.*

References

1. Chemical Reaction Engineering Module User's Guide. – COMSOL, 2020.
2. Ghasem N. Modeling and Simulation of Chemical Process Systems. - CRC Press, 2015. – 518 p.